## CSI 409: Conversion of NFAs to DFAs <br> Solutions to the sample problems

1. Consider the following NFA. The set of states, $Q$, is $\left\{q_{0}, q_{1}, q_{2}, q_{3}\right\}$. The initial state is $q_{0}$ and the accepting state is $q_{3}$. The alphabet is $\{a, b\}$.

|  | a | b | $\epsilon$ |
| :---: | :---: | :---: | :---: |
| $q_{0}$ | $\emptyset$ | $\left\{q_{1}\right\}$ | $\left\{q_{2}\right\}$ |
| $q_{1}$ | $\left\{q_{2}\right\}$ | $\left\{q_{3}\right\}$ | $\emptyset$ |
| $q_{2}$ | $\emptyset$ | $\emptyset$ | $\left\{q_{1}\right\}$ |
| $q_{3}$ | $\emptyset$ | $\emptyset$ | $\emptyset$ |

Convert this NFA to a DFA.

2. Convert the following NFA to a DFA. The set of states, $Q$, is $\left\{q_{0}, q_{1}, q_{2}\right\}$. The initial state is $q_{0}$ and the accepting state is $q_{1}$. The alphabet is $\{a, b\}$.

|  | a | b | $\epsilon$ |
| :---: | :---: | :---: | :---: |
| $q_{0}$ | $\left\{q_{1}, q_{2}\right\}$ | $\emptyset$ | $\left\{q_{2}\right\}$ |
| $q_{1}$ | $\left\{q_{0}\right\}$ | $\left\{q_{1}\right\}$ | $\emptyset$ |
| $q_{2}$ | $\emptyset$ | $\emptyset$ | $\left\{q_{0}\right\}$ |


3. Convert the following NFA to a DFA. The set of states, $Q$, is $\{1,2,3\}$. The initial state is 1 and the accepting state is 3 . The alphabet is $\{a, b\}$.

4. Consider the following NFA. The set of states, $Q$, is $\{1,2,3\}$. The initial state is 1 and the accepting state is 2 . The alphabet is $\{a, b\}$.

|  | a | b | $\epsilon$ |
| :---: | :---: | :---: | :---: |
| 1 | $\{2,3\}$ | $\}$ | $\{2\}$ |
| 2 | $\}$ | $\}$ | $\}$ |
| 3 | $\{1\}$ | $\{2\}$ | $\}$ |



Convert this NFA to a DFA. Show work clearly.


