

# Discerning Canonical User Representation for Cross-Domain Recommendation



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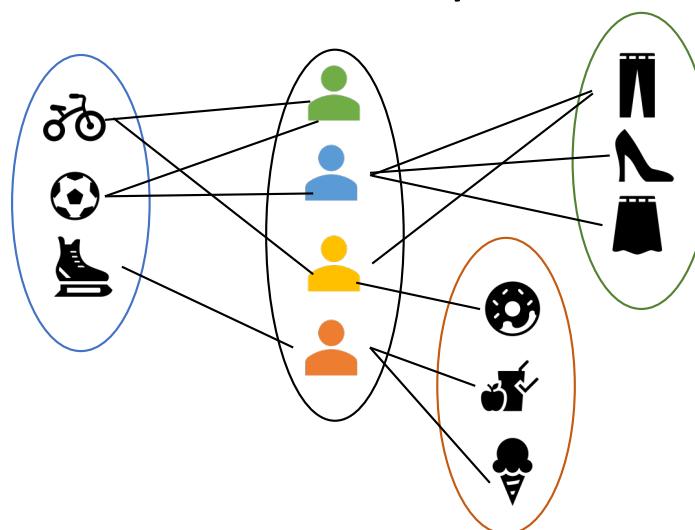


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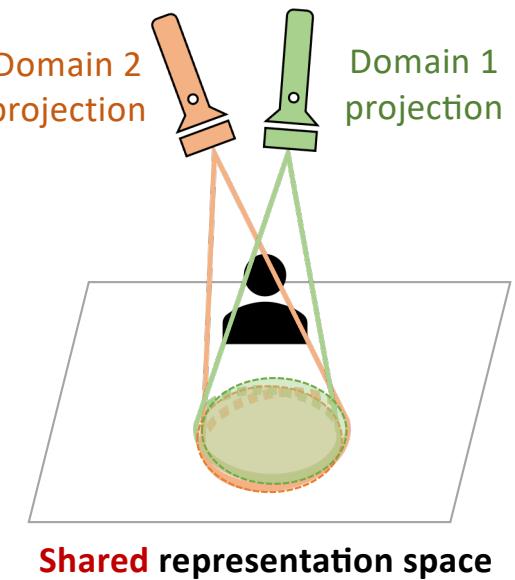
# Cross-domain recommender systems (CDRs)

- Transferring information across domains [Fernández-Tobías et. al. 2012]
  - Addressing data sparsity and the cold-start issues
  - Improving the quality of recommendations
- Assuming some user interest similarity across domains



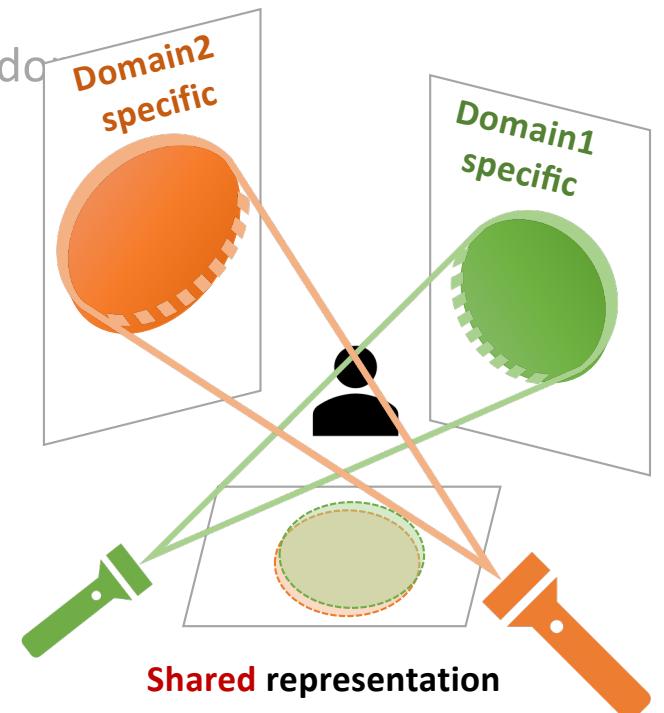
# User representation similarity across domains

- Complete overlap
  - Same or similar user representation **shared** across domains
  - Too restricted



# User representation similarity across domains

- Complete overlap
  - Same or similar user representation shared across domains
- Some overlap
  - **Domain-shared representation**
    - Information sharing between domains
  - **Domain-specific representation**
    - Representing unique user interests within each domain
  - Unbalanced freedom



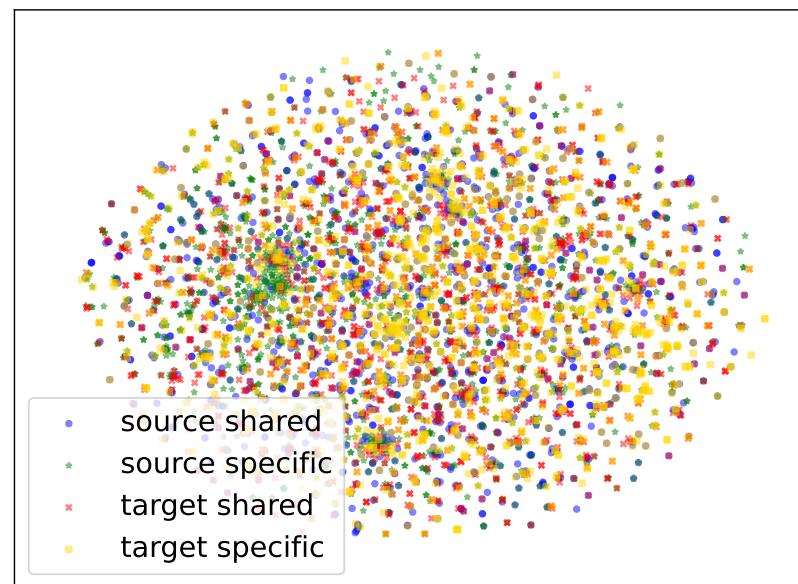
# Imbalance between domain specific & shared

- Over-restriction of domain-shared representations

- Free representations of domain disparities

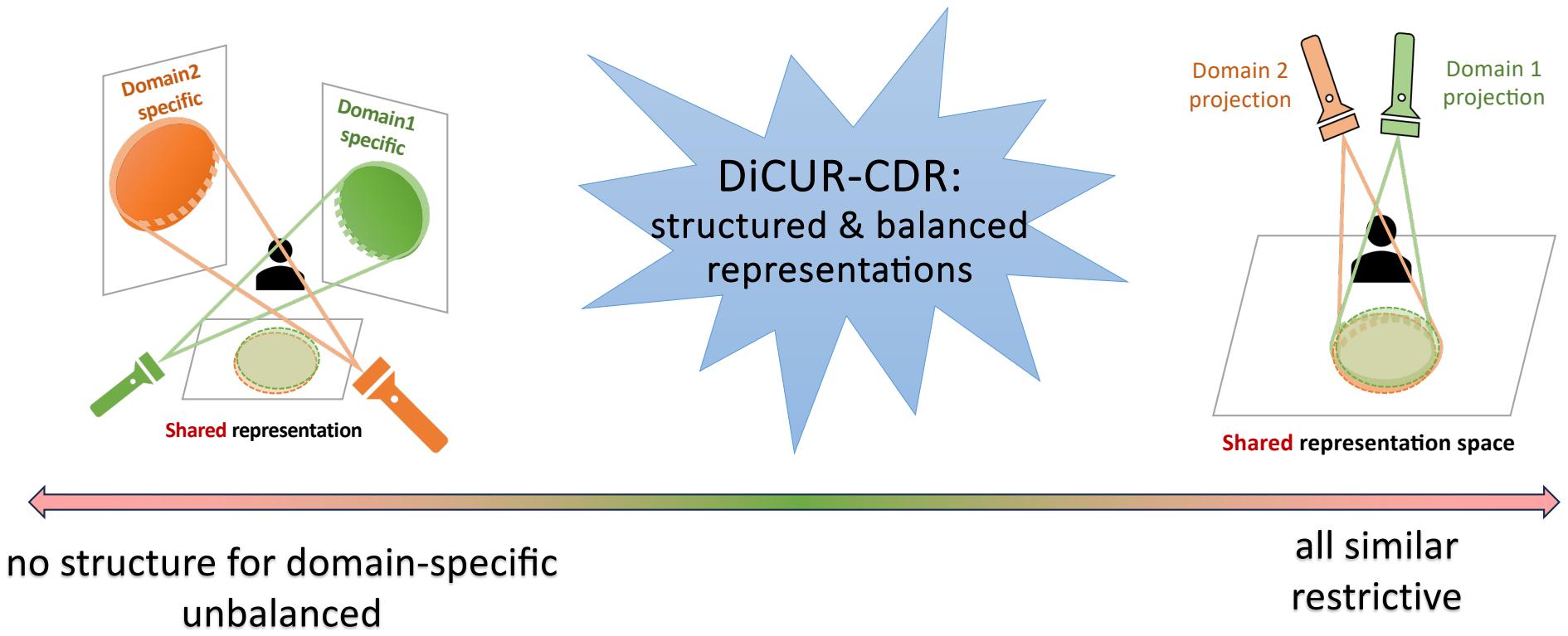


- Pushing **most** of the **information** into **domain-specific** representations
- Can't differentiate Domain-specific and domain-shared representations



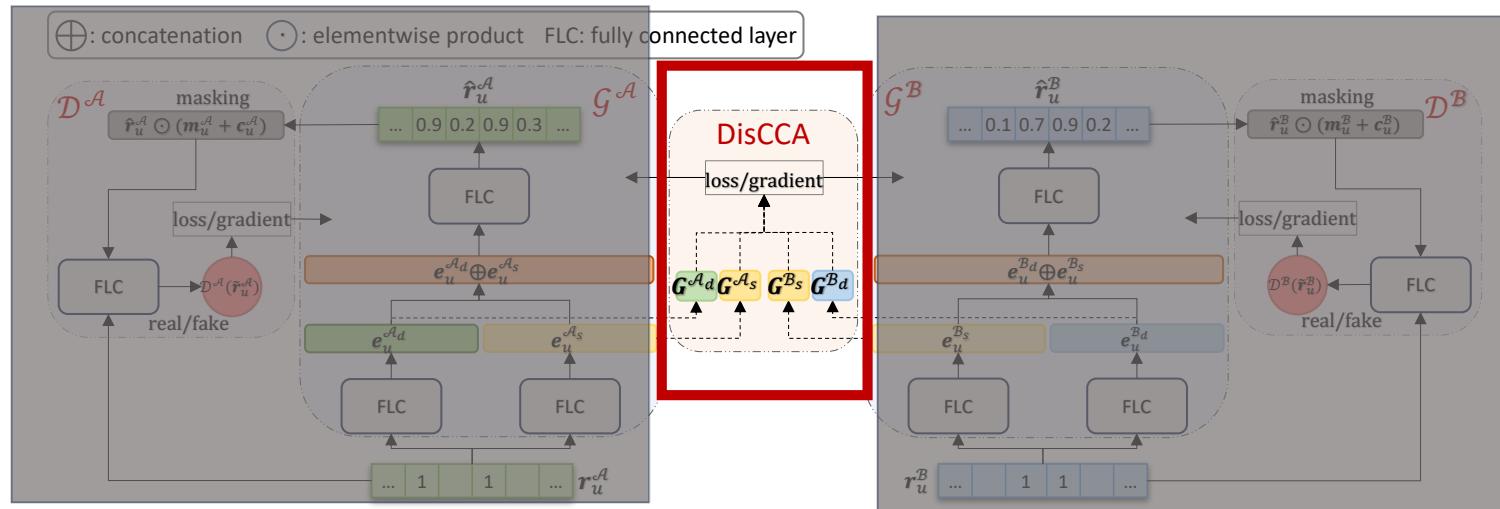
T-SNE of DisenCDR [Cao et al., 22] User Representations

# Our solution: DiCUR-CDR



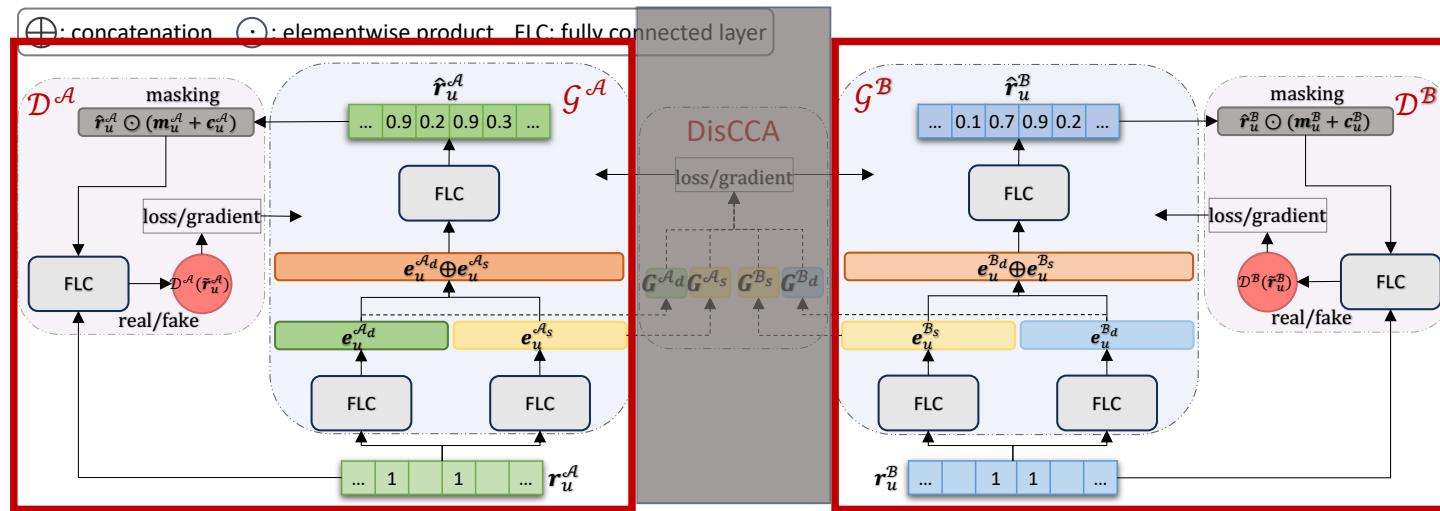
# Discerning Canonical User Representation Learning for Cross-Domain Recommendation (DiCUR-CDR)

- Discerning Canonical Correlation (DisCCA) user representation learning
- Generative adversarial learning to model user preferences and generate recommendations



# Discerning Canonical User Representation Learning for Cross-Domain Recommendation (DiCUR-CDR)

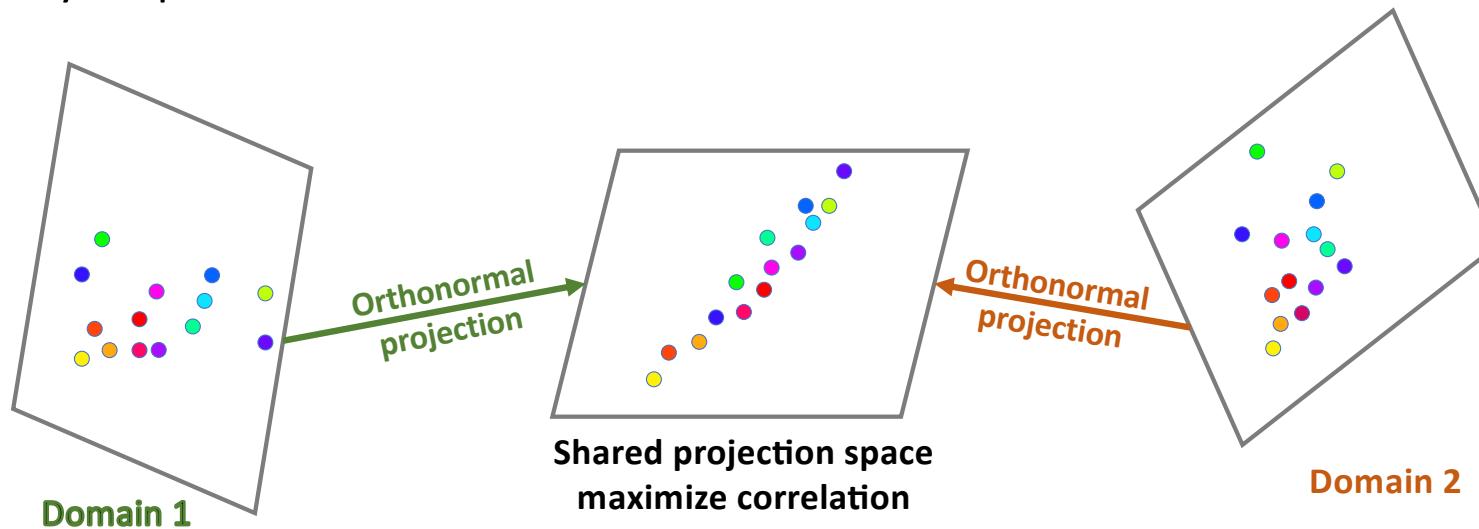
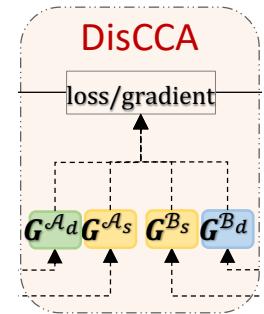
- Discerning Canonical Correlation (DisCCA) user representation learning
- Generative adversarial learning to model user preferences and generate recommendations



# Discerning Canonical Correlation - Background

Canonical Correlation Analysis (CCA) [Michel van de Velden, 2011]

- Maximize the linear correlation between multivariate variables
- Keep an orthonormal projection space
- Only maps “similarities” [Sahebi & Brusilovsky, 2016]

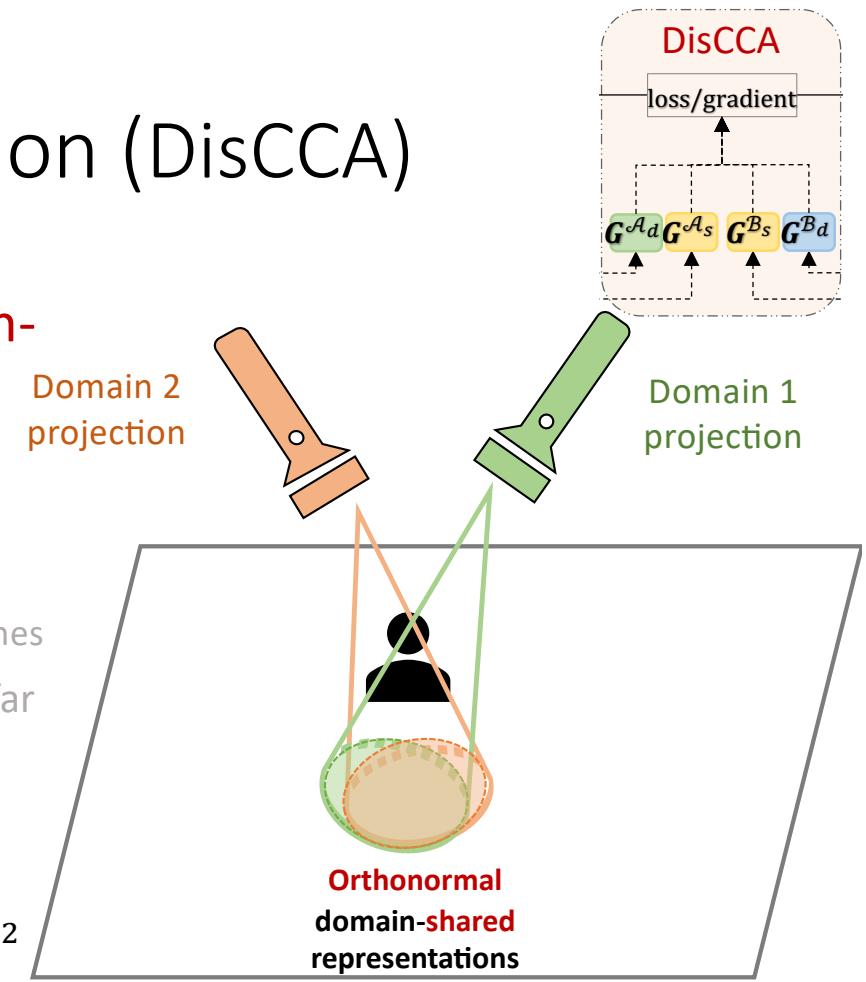


# Discerning Canonical Correlation (DisCCA)

- Maximize the correlation between **domain-shared** user representations
  - Keep an orthonormal projection space
- Maximize the disparities between domain-specific representations
  - Structured: Using the same projections as domain-shared ones
- Keep the domain-shared and domain-specific projections far apart

$$G^{\mathcal{A}_s} = LRelu(\mathbf{M}^{\mathcal{A}} \mathbf{e}^{\mathcal{A}_s}) \quad G^{\mathcal{B}_s} = LRelu(\mathbf{M}^{\mathcal{B}} \mathbf{e}^{\mathcal{B}_s})$$

$$\mathcal{L}_s = \|G^{\mathcal{A}_s} - G^{\mathcal{B}_s}\|^2 + \|G^{\mathcal{A}_s T} G^{\mathcal{A}_s} - I\|^2 + \|G^{\mathcal{B}_s T} G^{\mathcal{B}_s} - I\|^2$$

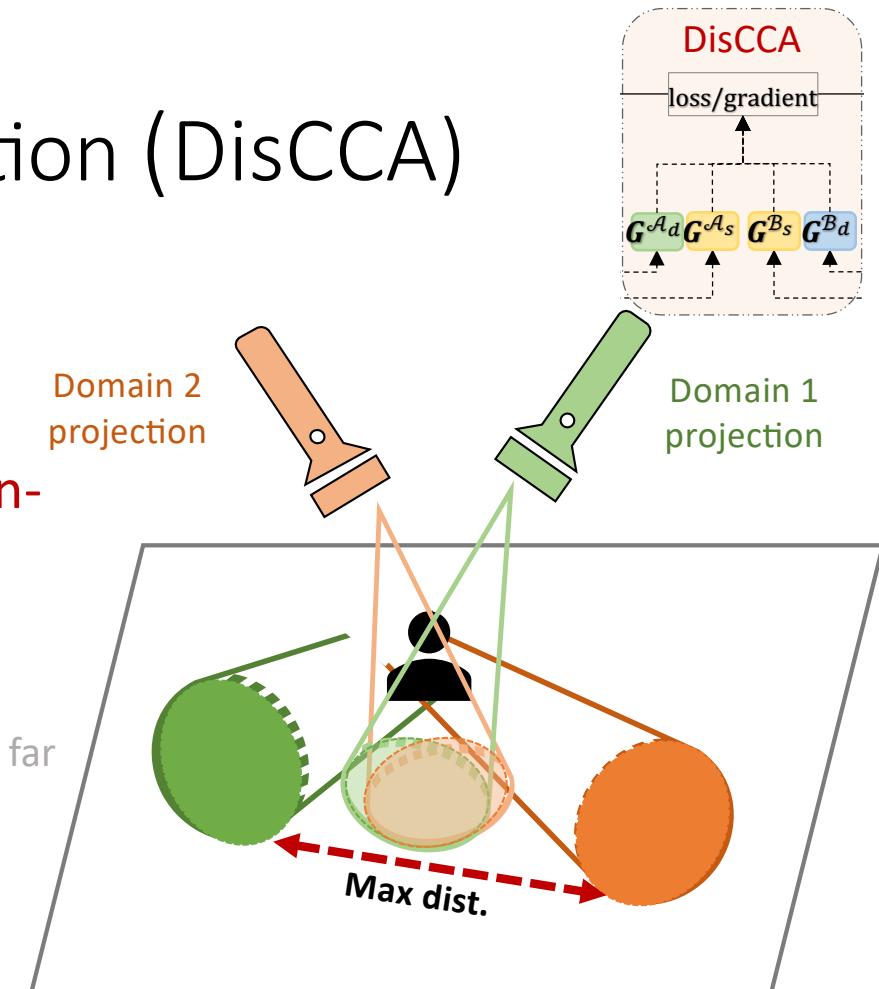


# Discerning Canonical Correlation (DisCCA)

- Maximize the correlation between domain-shared user representations
  - Keep an orthonormal projection space
- **Maximize the disparities between domain-specific representations**
  - **Structured:** Using the same correlation projections as domain-shared ones
- Keep the domain-shared and domain-specific projections far apart

$$G^{\mathcal{A}_d} = LRelu(\mathbf{M}^{\mathcal{A}} \mathbf{e}^{\mathcal{A}_d}) \quad G^{\mathcal{B}_d} = LRelu(\mathbf{M}^{\mathcal{B}} \mathbf{e}^{\mathcal{B}_d})$$

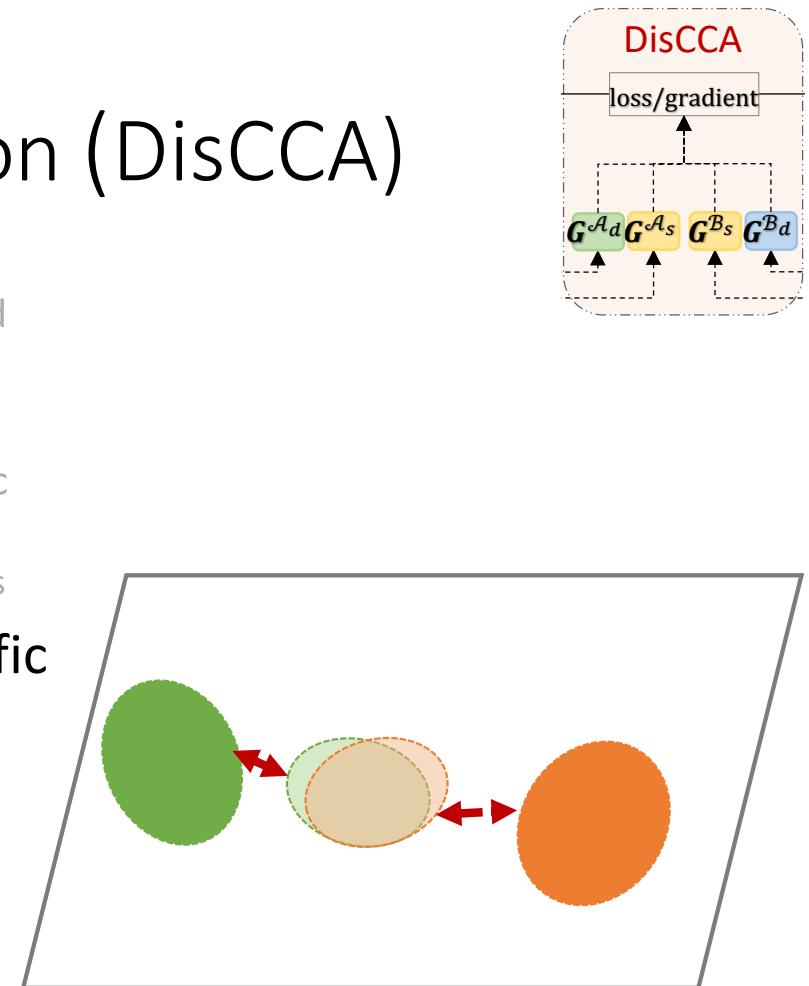
$$\mathcal{L}_d = \dots + \|G^{\mathcal{A}_d} - G^{\mathcal{B}_d}\|^2$$



# Discerning Canonical Correlation (DisCCA)

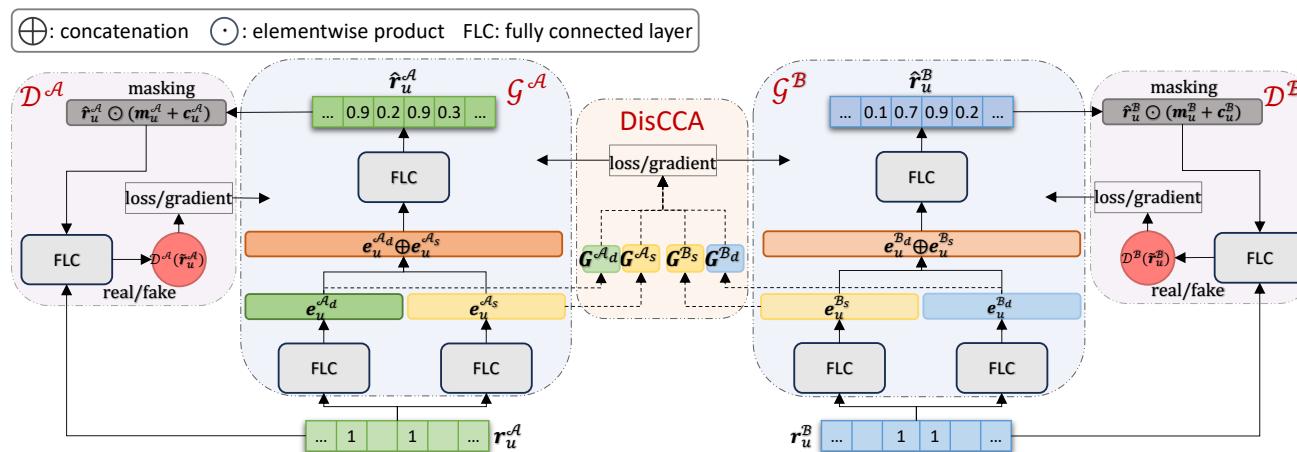
- Maximize the non-linear correlation between domain-shared user representations
  - Keep an orthonormal projection space
- Maximize the non-linear disparities between domain-specific representations
  - Structured: Using the same projections as domain-shared ones
- **Keep the domain-shared and domain-specific projections far apart**

$$\mathcal{L}_d = \|G^{\mathcal{A}_s} - G^{\mathcal{A}_d}\|^2 + \|G^{\mathcal{B}_s} - G^{\mathcal{B}_d}\|^2 + \dots$$



# DiCUR-CDR

- GAN for each domain
  - Generator ( $\mathcal{G}$ ): generates implicit feedback vectors
  - Discriminator ( $\mathcal{D}$ ): differentiates between the actual & generated feedback vectors



# DiCUR-CDR Model – GAN

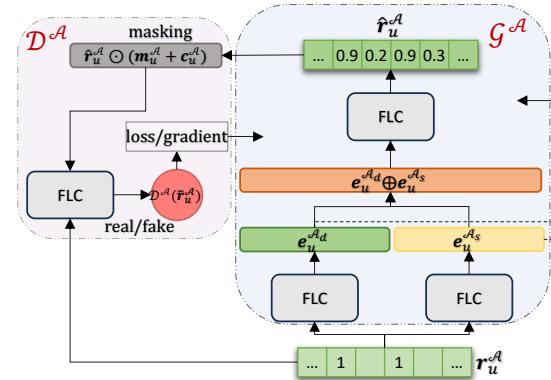
- Generator:

- Learning Domain-Shared & domain-Specific Representation
  - Fully-connected layer:

$$\begin{aligned} \mathbf{e}_u^{\mathcal{A}_d} &= \delta(\mathbf{W}_d^{\mathcal{A}} \mathbf{r}_u^{\mathcal{A}} + \mathbf{b}_d^{\mathcal{A}}) & \mathbf{e}_u^{\mathcal{B}_d} &= \delta(\mathbf{W}_d^{\mathcal{B}} \mathbf{r}_u^{\mathcal{B}} + \mathbf{b}_d^{\mathcal{B}}) \\ \mathbf{e}_u^{\mathcal{A}_s} &= \delta(\mathbf{W}_s^{\mathcal{A}} \mathbf{r}_u^{\mathcal{A}} + \mathbf{b}_s^{\mathcal{A}}) & \mathbf{e}_u^{\mathcal{B}_s} &= \delta(\mathbf{W}_s^{\mathcal{B}} \mathbf{r}_u^{\mathcal{B}} + \mathbf{b}_s^{\mathcal{B}}) \end{aligned}$$

- Recommendation Prediction
  - Fully-connected layer:

$$\begin{aligned} \hat{\mathbf{r}}_u^{\mathcal{A}} &= \mathcal{G}^{\mathcal{A}}(\mathbf{r}_u^{\mathcal{A}}) = \mathbf{W}_o^{\mathcal{A}} [\mathbf{e}_u^{\mathcal{A}_d} \oplus \mathbf{e}_u^{\mathcal{A}_s}] + \mathbf{b}_o^{\mathcal{A}} \\ \hat{\mathbf{r}}_u^{\mathcal{B}} &= \mathcal{G}^{\mathcal{B}}(\mathbf{r}_u^{\mathcal{B}}) = \mathbf{W}_o^{\mathcal{B}} [\mathbf{e}_u^{\mathcal{B}_d} \oplus \mathbf{e}_u^{\mathcal{B}_s}] + \mathbf{b}_o^{\mathcal{B}} \end{aligned}$$

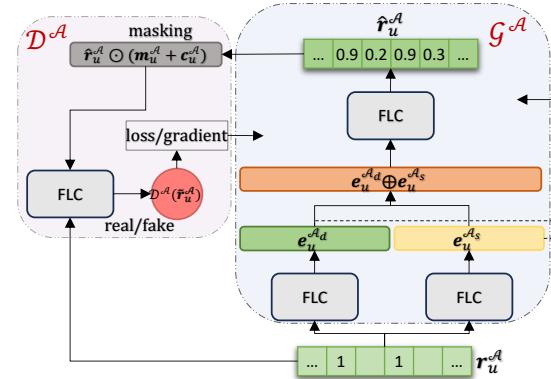


# DiCUR-CDR Model – GAN

- Discriminator:
  - Estimating the probability of  $\tilde{\mathbf{r}}_u^A$  and  $\tilde{\mathbf{r}}_u^B$  being real

$$\mathcal{D}^A(\tilde{\mathbf{r}}_u^A) = \delta(\mathbf{W}_n^A [\mathbf{r}_u^A \oplus (\tilde{\mathbf{r}}_u^A \odot \mathbf{m}_u^A)] + \mathbf{b}_n^A)$$

$$\mathcal{D}^B(\tilde{\mathbf{r}}_u^B) = \delta(\mathbf{W}_n^B [\mathbf{r}_u^B \oplus (\tilde{\mathbf{r}}_u^B \odot \mathbf{m}_u^B)] + \mathbf{b}_n^B)$$



# DiCUR-CDR Model – Learning

- Negative Sampling
  - Randomly selecting  $\omega$  (hyperparameter) portion of the unobserved items as the negative items ( $N_u^A$  and  $N_u^B$ )
  - Generating values close to 1 for the observed items
  - Producing low values for the negative ones.

- Generators loss:

$$\tilde{\mathcal{L}}_{G^A} = \sum_u \log \left( 1 - \mathfrak{D}^A(\tilde{\mathbf{r}}_u^A) \right) + \lambda_s \mathcal{L}_s + \lambda_d \mathcal{L}_d + \lambda_\theta \left\| \theta_{G^A} \right\|^2 + \lambda_n \left\| (\mathbf{r}_u^A - \hat{\mathbf{r}}_u^A) \odot (\mathbf{m}_u^A + \mathbf{c}_u^A) \right\|^2$$

- Discriminators loss:

$$\mathcal{L}_{D^A} = - \sum_u \left( (\log \left( \mathfrak{D}^A(\mathbf{r}_u^A) \right) + \log \left( 1 - \mathfrak{D}^A(\tilde{\mathbf{r}}_u^A) \right)) + \lambda_\theta \left\| \theta_{D^A} \right\|^2 \right)$$

# Experiments

- Five sets of experiments
  -  • Recommendation Prediction
  -  • Ablation Studies
  -  • Sensitivity Analysis
  -  • Cold-start Analysis
  -  • Learned User Representations Visualization



# Comparison with Baselines

Dataset			Amazon						Yelp					
Domain	Movies_and_TV			Video_Games			Restaurants			Shopping				
Metrics	HR	NDCG	MRR											
CDAE	0.33568**	0.24340**	0.20778**	0.27396**	0.17902**	0.14791**	0.42771**	0.27756**	0.22832**	0.25556**	0.17131**	0.14367**		
IRGAN	0.33157**	0.23693**	0.23222**	0.31791**	0.22461**	0.20295**	0.50491**	0.34964**	0.18901**	0.26976**	0.17966**	0.08962**		
DASO	0.33214**	0.23944**	0.20377**	0.27104**	0.17747**	0.14681**	0.42239**	0.28516**	0.24051**	0.26000**	0.17447**	0.14645**		
CDAE w/ M	0.33682**	0.24455**	0.20892**	0.27380**	0.17975**	0.14895**	0.41352**	0.26338**	0.21457**	0.27420**	0.17848**	0.14711**		
IRGAN w/ M	0.31626**	0.22674**	0.22717**	0.30294**	0.22136**	0.07760**	0.50211**	0.28131**	0.14198**	0.26799**	0.17900**	0.08785**		
DASO w/ M	0.32930**	0.23862**	0.20363**	0.26440**	0.17027**	0.13954**	0.42061**	0.28853**	0.24503**	0.18191**	0.11756**	0.09665**		
CoNet	0.37387**	0.32448**	0.27704**	0.37507**	0.24989**	0.20206**	0.49308**	0.26150**	0.17489**	0.24183**	0.09057**	0.07780**		
DDTCDR	0.41748**	0.34188**	0.29904**	0.38964**	0.27384**	0.23580**	0.54020**	0.41304**	0.36528**	0.32191**	0.20618**	0.16825**		
ETL	0.43038**	0.30931**	0.37091**	0.40373**	0.27032**	0.35928**	0.56406**	0.43037*	0.35102**	0.37265**	0.26387**	0.23093**		
DisenCDR	0.44062**	0.33783**	0.18056**	0.47047**	0.32741**	0.21987**	0.55993**	0.38873**	0.33760**	0.44191**	0.30617**	0.29475**		
CAT-ART	0.50733*	0.40527**	0.37043**	0.49988*	0.38892**	0.35217**	0.59800*	0.42238**	0.36446**	0.51718*	0.37004*	0.32146*		
DiCUR-CDR	<b>0.51235</b>	<b>0.42119</b>	<b>0.39360</b>	<b>0.51006</b>	<b>0.40646</b>	<b>0.37303</b>	<b>0.61548</b>	<b>0.43752</b>	<b>0.37968</b>	<b>0.52833</b>	<b>0.37740</b>	<b>0.32785</b>		

Recommendation Performance Prediction results, \*\* and \* indicate t-test p – value < 0.05 and p – value < 0.1

- DiCUR-CDR **outperforms all baselines** across **both datasets** and **domains**
  - Demonstrating the **feasibility** of incorporating **DisCCA**



# Ablation Studies: all discerning representations matter

Dataset	Amazon						Yelp					
Domain	Movies_and_TV			Video_Games			Restaurants			Shopping		
Metrics	HR	NDCG	MRR									
DiCUR-CDR w/o S	0.47833	0.40129	0.37589	0.50196	0.40057	0.36784	0.60478	0.43682	0.38292	0.51604	0.37253	0.32563
DiCUR-CDR w/o D	0.47914	0.40216	0.37679	0.50344	0.40116	0.36771	0.60205	0.42718	0.37165	0.51877	0.37640	0.32631
DiCUR-CDR w/o S&D	0.47578	0.39918	0.37381	0.49627	0.39939	0.36730	0.60000	0.42964	0.37513	0.51809	0.37242	0.32579
DiCUR-CDR w/o GAN (MLP w/ DisCCA)	0.47253	0.39982	0.37671	0.44026	0.36168	0.33622	0.5372	0.39011	0.34272	0.4942	0.36145	0.31926
DiCUR-CDR	<b>0.51235</b>	<b>0.42119</b>	<b>0.39360</b>	<b>0.51006</b>	<b>0.40646</b>	<b>0.37303</b>	<b>0.61548</b>	<b>0.43752</b>	<b>0.37968</b>	<b>0.52833</b>	<b>0.37740</b>	<b>0.32785</b>

Ablation study results

- Removing either  $\mathcal{L}_S$  or  $\mathcal{L}_D$ , or both, leads to a performance decline
  - Distinguishing between domain-shared & domain-specific representation, ensuring distinct domain-specific representations, are all crucial



# Ablation Studies: GAN matters

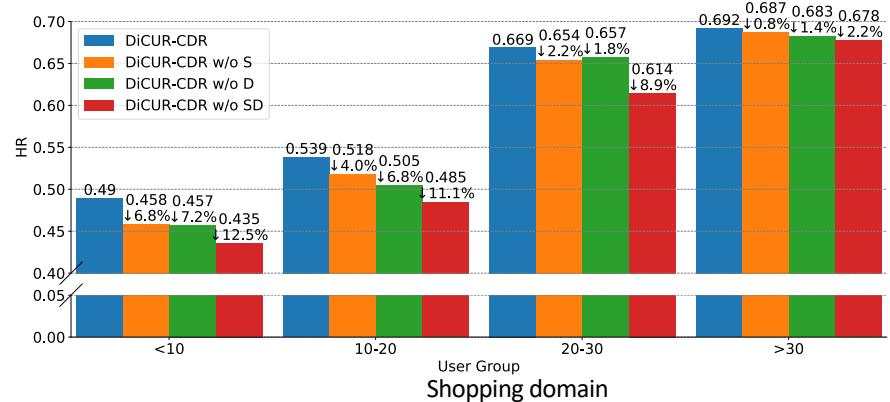
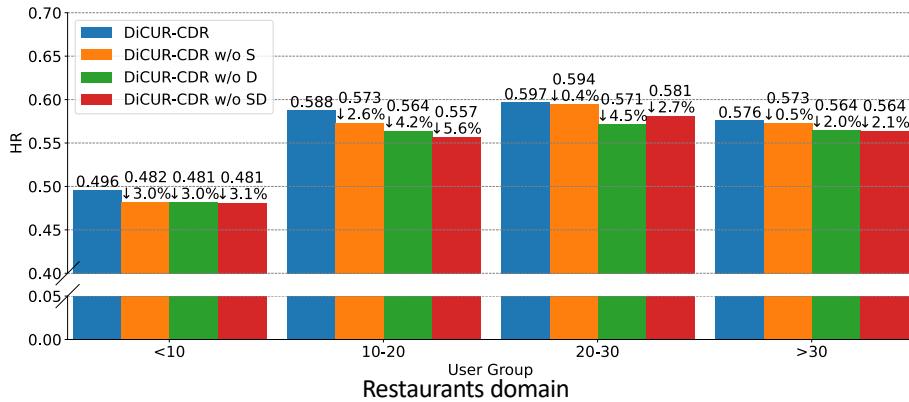
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Ablation study results

- DiCUR-CDR w/o GAN exhibits the **lowest** performance
  - Highlighting the **effectiveness** of using **GAN**



# Cold-start Analysis

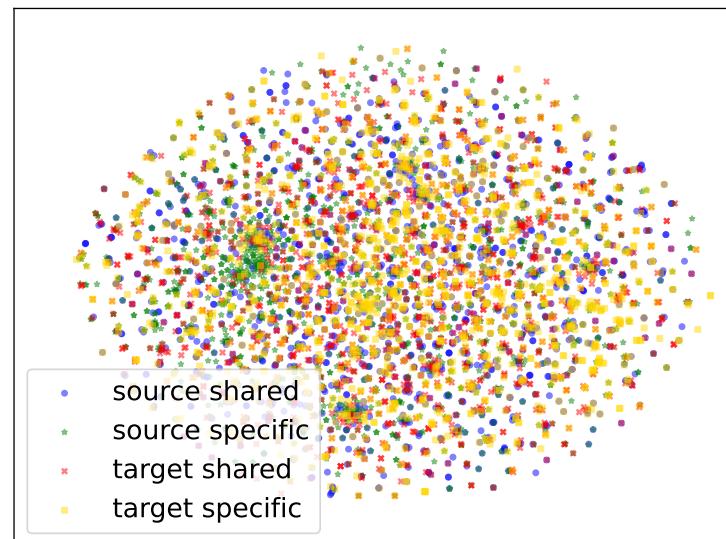
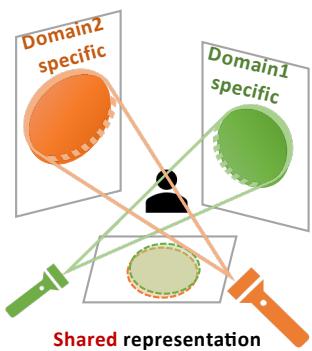


Recommendation results (HR) for users with different numbers of interactions on the Yelp dataset

- The largest recommendation prediction improvements happen for
  - users with fewer interactions (groups < 10 and 10 – 20)
  - sparser domain



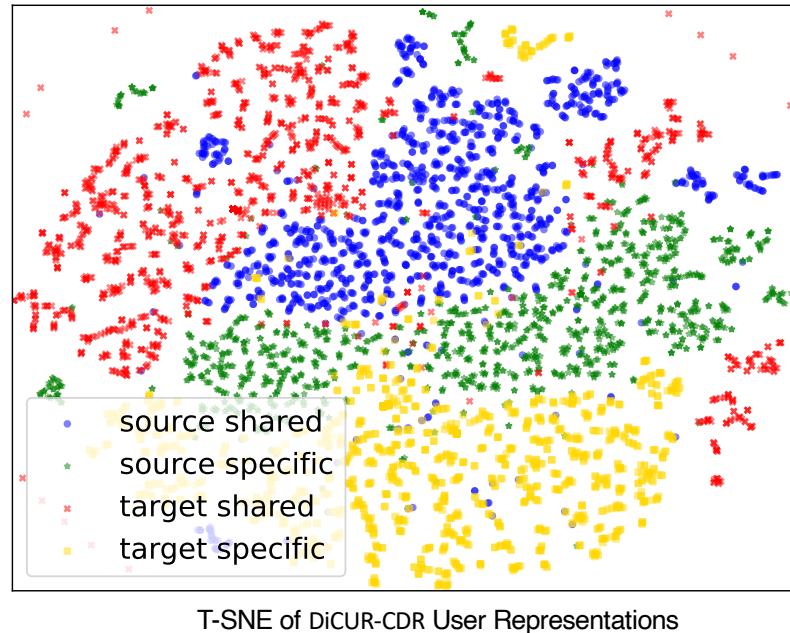
# Baseline Learned User Representations



T-SNE of DisenCDR [Cao et al., 22] User Representations



# DiCUR-CDR Learned User Representations



Pushing the **domain-shared** representations **close** to each other  
Separating and differentiating between the **domain-specific** ones

# Conclusions

- Proposed Discerning Canonical User Representation Learning for Cross-Domain Recommendation (DiCUR-CDR)
- Introduced Discerning Canonical Correlation (DisCCA) user representation learning
- Emphasized the effectiveness of
  - Capturing both cross-domain and within-domain user preferences
  - Discerning the domain-specific representations in a structured way



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# Thank you! Q & A



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Our code and sample data are available at GitHub:  
<https://github.com/persai-lab/2024-RecSys-DiCUR-CDR>